

To Study Alternative to Segmental Box Girder Superstructure

AKSHYA KUMAR SALUNKHE¹ and M. M. MAHAJAN²

¹M.Tech Scholar, VNIT Nagpur

²Professor, VNIT Nagpur

E-mail: ¹salunkheakshya94@gmail.com, ²mukundmmahajan@gmail.com

Abstract—Performance based selection of bridge superstructure is important for economy and longevity of structure and ease of construction. It is observed that construction resources influence the execution of a bridge and time of construction.

In this project a case study of a Bridge at Sarai Kale Khan area of New Delhi, on Barapullah Nallah has been taken for the academic purpose. Study of the existing Segmental Box girder Superstructure has been done and Alternatives are given as below:

- Alternative: 4 number of girder Simply Supported structure.

The structures are modeled in MIDAS Civil software and studied for various loading conditions as per IRC:6-2014 and IRC:112-2011. The construction stages analyses and time dependent analyses are also done using MIDAS Civil.

Index Terms—Segmental Box Girder Superstructure, Simply Supported Girder, Construction Stages, MIDAS Civil Software.

1. Introduction

The various construction stages are considered for analysis in MIDAS for Simply Supported Structure:

Stage (1,1) represents Self-weight of girder and first stage of prestressing before launching of the girder. (at Transfer stage).

Stage (1,2) represents casting of deck slab after launching of the Girder.

Stage (2,1) represents after 7 days of deck slab casting.

Stage (2,2) represents second stage of prestressing on composite structure after 28 days of deck slab casting.

Stage (3,1) represents placing of SIDL fix and variable after second stage of prestressing done. (@ Service stage).

Stage (3,2) represents after 30 years of the bridge constructed.

2. Existing Segmental Box Girder Super structure.

The Barapullah Phase II: consists of a 3 span continuous prestressed bridge. It is a precast segmental bridge structure consisting of five post tensioned prestressing tendons (in each web). Three out of which are placed throughout the length and remaining two are placed at support to minimize the support negative moments.

Construction Methodology:

The stages of construction as well as the longitudinal arrangement of the segments are represented in Figure 2.1 It also shows the bearing types at different piers.

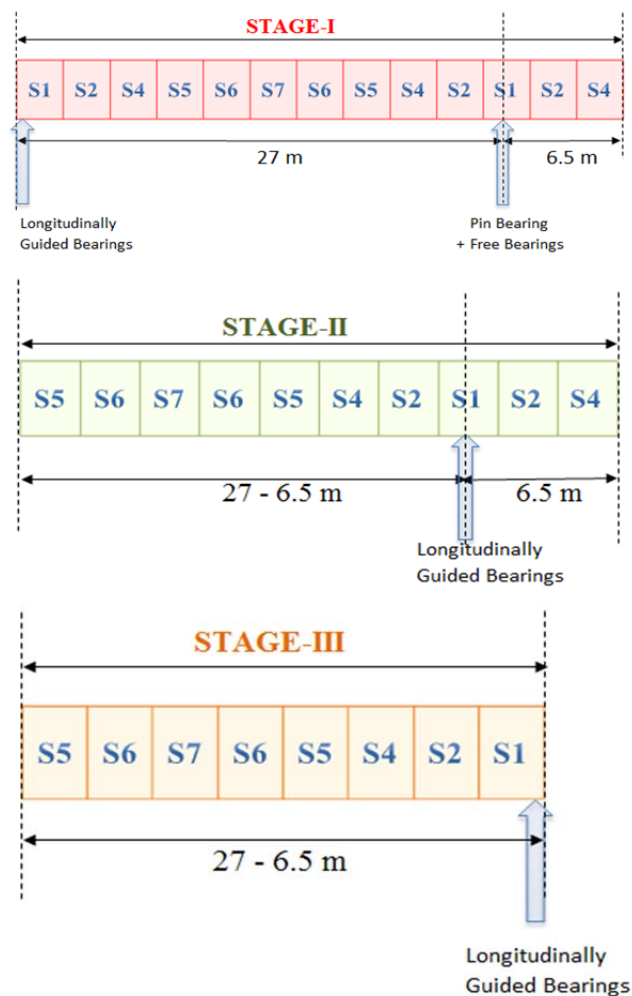


Figure 2.1 Construction Stages for 3-span continuous bridge

Definition of Cable Profile:

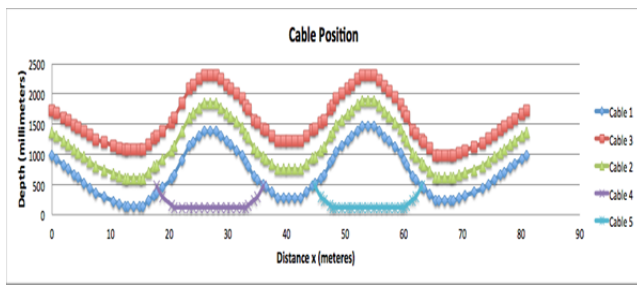


Figure 2.2 Cable Positioning according to the depth of Box Girder.

| Structural Properties | Continuous Model | | | | | | | | | | | |
|---------------------------------------|------------------|------|------|------|---------|------|------|------|---------|------|------|------|
| | Stage 1 | | | | Stage 2 | | | | Stage 3 | | | |
| | S1 | S4 | S6 | S1B | S1 | S4 | S6 | S1B | S1 | S4 | S6 | S1B |
| Depth (m) | 2.45 | | | | 2.45 | | | | 2.45 | | | |
| A (m ²) | 8.39 | 5.2 | 4.84 | 9.03 | 8.39 | 5.2 | 4.84 | 9.03 | 8.39 | 5.2 | 4.84 | 9.03 |
| Y _{top} (mm) | 1021 | 858 | 829 | 1019 | 1021 | 858 | 829 | 1019 | 1021 | 858 | 829 | 1019 |
| Y _{bottom} (mm) | 1429 | 1592 | 1621 | 1431 | 1429 | 1592 | 1621 | 1431 | 1429 | 1592 | 1621 | 1431 |
| I _{xx} (m ⁴) | 5.76 | 3.97 | 3.79 | 5.95 | 5.76 | 3.97 | 3.79 | 5.95 | 5.76 | 3.97 | 3.79 | 5.95 |
| Z _{top} (m ³) | 5.64 | 4.63 | 4.57 | 5.85 | 5.64 | 4.63 | 4.57 | 5.85 | 5.64 | 4.63 | 4.57 | 5.85 |
| Z _{bottom} (m ³) | 4.03 | 2.50 | 2.34 | 4.15 | 4.03 | 2.50 | 2.34 | 4.15 | 4.03 | 2.50 | 2.34 | 4.15 |

Table 2.1 Sectional Properties of Continuous Segmental Box Girder:

Prestress Force:

Prestressing force as per cable profile including the losses has been applied. The high tensile steel for prestressing shall consist of uncoated, stress relieved, low relaxation strands conforming to class II of IS: 14268-1995 (with a breaking load of 260.7 kN for 15.2 mm strand).

Table 2.2 Prestressing Cable properties:

| | |
|--|---------------------|
| Wobble coefficient of the sheathing duct/strand | k = 0.002 per meter |
| Friction coefficient of the sheathing duct/strand | m = 0.17 per radian |
| Wedge slip at decking end | 6 mm |
| Type of cable | 19K15 |
| Type of sheaths | HDPE |
| Duct diameter | 105 mm |
| Minimum c/c distance between cables | 210 mm |
| Minimum distance of centre of cable from surface of concrete | 130 mm |

Mathematical Modelling:

The mathematical modeling of segmental PSC box Girder Bridge having span of (27+27+27) m is shown in Figure 3.15. The modeling of the bridge structure is done in MIDAS Civil Software (2016 version) and Beam Element is used for geometry and PSC single cell box is chosen as the cross section. Type of model is Linear Elastic modeling. Rigid links are used to transfer the forces to the supports.

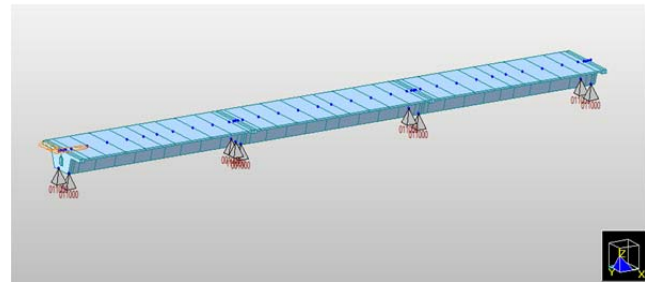


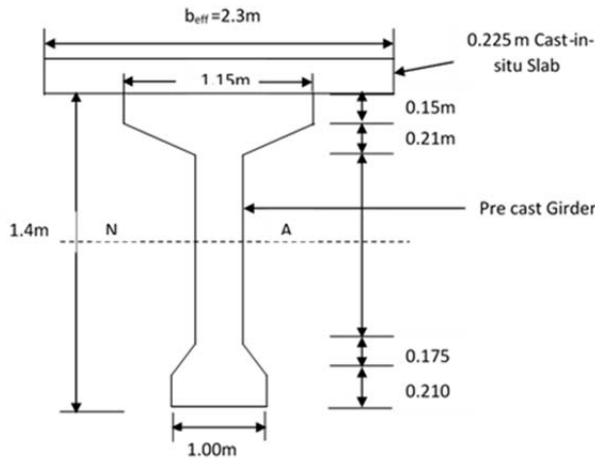
Figure 2.3 Modeling of Segmental Box Girder Superstructure in MIDAS Civil.

Table 2.3 Deflection Check:

| Deflection (mm) | | At Transfer | At Service | |
|-----------------|----------|-------------|------------|------|
| Stage 1 | S1 | 0 | - | |
| | S4 | 0.731 | | |
| | S6 | 1.19 | | |
| | Couplers | -1.275 | | |
| Stage 2 | S1 | 0 | | |
| | S4 | 0.913 | | |
| | S6 | 1.045 | | |
| | Coupler | -1.032 | | |
| Stage 3 | S1 | 0 | | 0 |
| | S4 | 3.17 | | 0.98 |
| | S6 | 4.27 | -1.05 | |

Table 2.4 Check for stresses at top and bottom at both transfer and service stage:

| Design Output Stresses (MPa) | Stage 1 | | | | Stage 2 | | | | Stage 3 | | | | |
|------------------------------|---------------------|-----|-----|-----|---------|-----|-----|-----|---------|-----|-----|-----|-----|
| | S1 | S4 | S6 | S1B | S1 | S4 | S6 | S1B | S1 | S4 | S6 | S1B | |
| At Transfer | σ _{top} | 1.3 | 2.7 | 2.8 | 1.2 | 1.3 | 2.6 | 2.6 | 0.8 | 1.9 | 3.1 | 2.9 | 1.4 |
| | σ _{bottom} | 1.5 | 0.7 | 0.3 | 1.2 | 1.5 | 1.0 | 0.8 | 1.8 | 2.2 | 2.8 | 3.1 | 2.9 |
| At Service | σ _{top} | - | | | | | | | | 1.9 | 4.3 | 4.4 | 0.7 |
| | σ _{bottom} | - | | | | | | | | 2.2 | 0.6 | 0.2 | 3.9 |



Validation of MIDAS Civil Modeling:

Validation of modelling done in MIDAS Civil software with STAAD Pro software and Manual calculation in which distribution factor is calculated by using Courbon’s method is done.

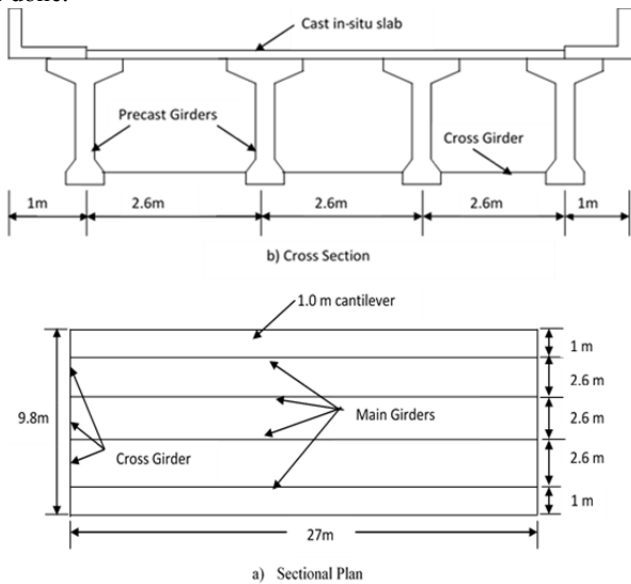


Figure 3.1 Plan and Cross section of Bridge Structure.

| | Class A (Edge) | Class A (Centre) | Class 70R (Centre) | Class 70R (Edge) | 2 lane Class A (Edge) |
|--------------------------|----------------|------------------|--------------------|------------------|-----------------------|
| Maxi. B.M. (kN-m) Manual | 1642 | 1147 | 2489 | 2565 | 2025 |
| Maxi. B.M. (kN-m) MIDAS | 1520 | 1119 | 2436 | 2394 | 1795 |

| Maxi. B.M. (kN-m) STAAD | 1522 | 1078 | 2300 | 2471 | 1962 |
|-------------------------|------|------|------|------|------|
|-------------------------|------|------|------|------|------|

Table 3.1 Maximum Bending Moment (kN-m)

comparison:

Table 4.4 Shows that there is maxi. Variation between MIDAS and STAAD results is 8.5%. Variation between MIDAS and Manual calculation result is 11.35%. it means that modeling in MIDAS is correct.

4. Alternative 4 number of girder Simply Supported structure:

3. Vehicular Live Load for clear carriageway of 9m is applied as per IRC: 6-2014. Following options were considered for the analysis of present problem.

- Class A Wheeled Vehicle – 1 Lane
- Class A Wheeled Vehicle – 2 Lane
- 70R Wheeled Vehicle – 1 Lane.

The impact factor for the appropriate loading class is considered as per IRC: 6-2014.

Figure 4.1 Cross section of Exterior Girder.

Table 4.1 Section Properties of exterior I-girder:

| Section Properties | I-Girder | | Composite I-Girder | |
|-----------------------------------|----------|----------|--------------------|----------|
| | Support | Mid-span | Support | Mid-span |
| Area (m ²) | 1.454 | 0.845 | 1.972 | 1.363 |
| Depth (m) | 1.40 | 1.40 | 1.625 | 1.625 |
| Y _b (m) | 0.72 | 0.71 | 0.93 | 1.01 |
| I _{xx} (m ⁴) | 0.243 | 0.200 | 0.486 | 0.409 |
| Z _t (m ³) | 0.357 | 0.290 | 0.700 | 0.665 |
| Z _b (m ³) | 0.337 | 0.282 | 0.522 | 0.405 |

Table 4.2 Variation of Moment and Shear Force along span for exterior I-girder:

| Properties | Exterior I-Girder | | | | | |
|-------------------------|-------------------|------|------|------|------|------|
| | Values | | | | | |
| Section from end | 0L | 0.1L | 0.2L | 0.3L | 0.4L | 0.5L |
| M _{DL} | 0 | 1296 | 2034 | 2743 | 3071 | 3229 |
| SF _{DL} | 493 | 367 | 287 | 183 | 105 | 0 |
| M _{SIDL-Fix} | 0 | 239 | 350 | 456 | 499 | 520 |
| SF _{SIDL-Fix} | 82 | 70 | 54 | 33 | 15 | 0 |
| M _{SIDL-Vari} | 0 | 152 | 242 | 326 | 365 | 383 |
| SF _{SIDL-Vari} | 58 | 44 | 35 | 22 | 13 | 0 |
| M _{Live} | 0 | 760 | 1260 | 1712 | 1910 | 2034 |
| SF _{Live} | 342 | 310 | 223 | 188 | 119 | 79 |

Table 4.3 Details of prestressing cable profile:

| Cable no. | Strand Type | Sheating Dia. (mm) | Jacking Stress (Mpa) | Y _{bottom} at sup. (mm) | Y _{bottom} at mid (mm) |
|-----------|-------------|--------------------|----------------------|----------------------------------|---------------------------------|
| C1 | 7PLY15 | 110 | 1267 | 1100 | 150 |
| C2 | 7PLY15 | 110 | 1267 | 700 | 150 |
| C3 | 7PLY15 | 110 | 1267 | 300 | 150 |

Table 4.4 Permissible stresses in concrete:

| Stress in concrete | Expression |
|---|---------------------|
| Compressive strength of concrete at transfer (f_{ci}) | $0.8 f_{ck}$ (32) |
| Permissible compressive stress in concrete at transfer (f_{ct}) | $0.5 f_{ci}$ (16) |
| Permissible tensile stress in concrete at transfer (f_{ti}) | 0 |
| Permissible compressive stress in concrete at working (f_{cw}) | $0.4 f_{ck}$ (12.8) |
| Permissible tensile stress in concrete at working (f_{tw}) | 0 |

| Properties | Values (Mpa) | | | | | |
|----------------------|--------------|------|------|-------|-------|-------|
| Section from end (m) | 0 | 2.7 | 5.4 | 8.1 | 10.8 | 13.5 |
| σ_{top} | 3.70 | 5.68 | 4.17 | 3.39 | 3.97 | 4.30 |
| σ_{bottom} | 4.34 | 8.12 | 9.86 | 10.95 | 10.48 | 10.26 |

Table 4.5 Check for stresses at construction stage (1,1) in exterior I-girder:

| Properties | Values (Mpa) | | | | | |
|----------------------|--------------|------|------|------|------|------|
| Section from end (m) | 0 | 2.7 | 5.4 | 8.1 | 10.8 | 13.5 |
| σ_{top} | 3.59 | 7.29 | 6.95 | 7.22 | 8.22 | 8.75 |
| σ_{bottom} | 4.14 | 5.80 | 6.31 | 6.30 | 5.42 | 4.99 |

Table 4.6 Check for stresses at construction stage (1,2) in exterior I-girder:

| Properties | Values (Mpa) | | | | | |
|----------------------|--------------|------|------|------|------|------|
| Section from end (m) | 0 | 2.7 | 5.4 | 8.1 | 10.8 | 13.5 |
| σ_{top} | 4.57 | 7.94 | 7.16 | 7.07 | 7.97 | 8.46 |
| σ_{bottom} | 6.65 | 11.1 | 12.8 | 13.6 | 12.9 | 12.5 |

Table 4.7 Check for stresses at construction stage (2,2) in exterior I-girder:

| Properties | Values (Mpa) | | | | | |
|----------------------|--------------|------|------|------|------|------|
| Section from end (m) | 0 | 2.7 | 5.4 | 8.1 | 10.8 | 13.5 |
| σ_{top} | 4.60 | 8.27 | 7.66 | 7.74 | 8.69 | 9.20 |
| σ_{bottom} | 6.50 | 9.91 | 11.0 | 11.3 | 10.4 | 10.0 |

Table 4.8 Check for stresses at construction stage (2,3) in exterior I-girder:

| Properties | Values (Mpa) | | | | | |
|----------------------|--------------|------|------|------|------|------|
| Section from end (m) | 0 | 2.7 | 5.4 | 8.1 | 10.8 | 13.5 |
| σ_{top} | 3.36 | 5.83 | 5.60 | 5.78 | 6.40 | 6.74 |
| σ_{bottom} | 6.17 | 8.80 | 9.33 | 9.33 | 8.59 | 8.22 |

Table 4.9 Check for stresses at construction stage (3,1) in exterior I-girder:

Table 4.10 Check for stresses at service stage (SLS) in exterior I girder:

| Properties | Values (Mpa) | | | | | |
|----------------------|--------------|------|------|------|------|------|
| Section from end (m) | 0 | 2.7 | 5.4 | 8.1 | 10.8 | 13.5 |
| σ_{top} | 3.35 | 5.82 | 5.59 | 5.77 | 6.39 | 6.74 |
| σ_{bottom} | 6.14 | 6.92 | 6.26 | 5.14 | 3.91 | 3.24 |

As all stress values in all construction stages are within permissible limit i.e. 16 Mpa and 12.8 Mpa compressive stresses in transfer stage and working stage respectively. 0 Mpa tensile stresses in all construction stages or there is no tensile stress at all in any stage.

Table 4.11 Check for deflection at various stages in exterior I girder:

| Stages | Deflection (mm) | | | | | |
|----------------------|-----------------|------|-------|-------|-------|-------|
| Section from end (m) | 0L | 0.1L | 0.2L | 0.3L | 0.4L | 0.5L |
| Stage (1,1) | 0 | 4.67 | 8.78 | 11.55 | 12.81 | 12.80 |
| Stage (1,2) | 0 | 2.40 | 4.53 | 5.72 | 6.04 | 6.03 |
| Stage (2,2) | 0 | 4.97 | 9.15 | 11.67 | 12.60 | 12.59 |
| Stage (2,3) | 0 | 5.07 | 9.27 | 11.76 | 12.65 | 12.64 |
| Stage (3,2) | 0 | 8.40 | 14.98 | 18.89 | 20.38 | 20.37 |

The above all deflection values are within limits 34mm i.e. (span/800) so, it is safe in deflection criteria.

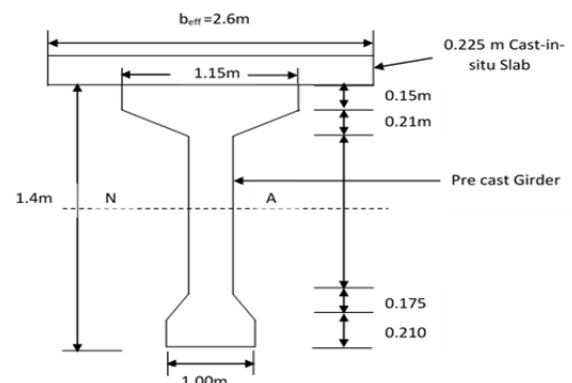


Figure 4.1 Cross section of Interior Girder

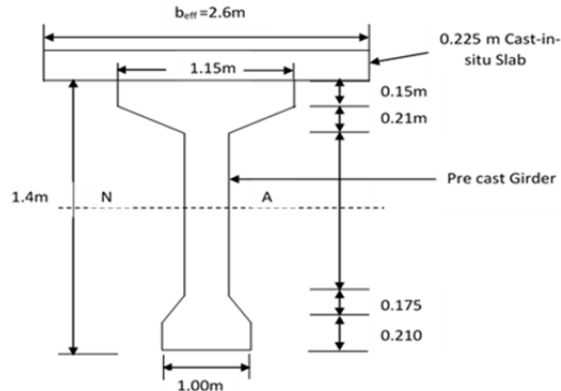


Table 4.12 Section Properties of Interior I-girder:

| Section Properties | I-Girder | | Composite I-Girder | |
|-----------------------------------|----------|----------|--------------------|----------|
| | Support | Mid-span | Support | Mid-span |
| Area (m ²) | 1.454 | 0.845 | 2.039 | 1.430 |
| Depth (m) | 1.40 | 1.40 | 1.625 | 1.625 |
| Y _b (m) | 0.72 | 0.71 | 0.95 | 1.04 |
| I _{xx} (m ⁴) | 0.243 | 0.200 | 0.508 | 0.425 |
| Z _t (m ³) | 0.357 | 0.290 | 0.753 | 0.726 |
| Z _b (m ³) | 0.337 | 0.282 | 0.535 | 0.409 |

Table 4.13 Variation of Moment and Shear Force along span for interior I-girder:

| Properties | Exterior I-Girder | | | | | |
|-------------------------|-------------------|------|------|------|------|------|
| | 0L | 0.1L | 0.2L | 0.3L | 0.4L | 0.5L |
| Section from end (m) | 0 | 2.7 | 5.4 | 8.1 | 10.8 | 13.5 |
| M _{DL} | 0 | 1286 | 2038 | 2757 | 3084 | 3244 |
| SF _{DL} | 503 | 373 | 295 | 187 | 107 | 0 |
| M _{SIDL-Fix} | 0 | 55 | 106 | 162 | 191 | 206 |
| SF _{SIDL-Fix} | 14 | 12 | 11 | 10 | 8 | 0 |
| M _{SIDL-Vari} | 0 | 150 | 239 | 325 | 365 | 384 |
| SF _{SIDL-Vari} | 55 | 44 | 35 | 22 | 13 | 0 |
| M _{Live} | 0 | 964 | 1473 | 1926 | 1982 | 2109 |
| SF _{Live} | 363 | 320 | 272 | 244 | 210 | 173 |

| Properties | Values (Mpa) | | | | | |
|----------------------|--------------|------|------|------|------|------|
| | 0 | 2.7 | 5.4 | 8.1 | 10.8 | 13.5 |
| Section from end (m) | 0 | 2.7 | 5.4 | 8.1 | 10.8 | 13.5 |
| σ _{top} | 3.70 | 5.68 | 4.17 | 3.39 | 3.97 | 4.30 |
| σ _{bottom} | 4.34 | 8.12 | 9.86 | 10.9 | 10.5 | 10.3 |

Table 4.14 Check for stresses at construction stage (1,1) in interior I-girder:

| Properties | Values (Mpa) | | | | | |
|----------------------|--------------|------|------|------|------|------|
| | 0 | 2.7 | 5.4 | 8.1 | 10.8 | 13.5 |
| Section from end (m) | 0 | 2.7 | 5.4 | 8.1 | 10.8 | 13.5 |
| σ _{top} | 3.55 | 7.28 | 6.90 | 7.09 | 8.08 | 8.61 |
| σ _{bottom} | 4.13 | 5.72 | 6.32 | 6.41 | 5.54 | 5.09 |

Table 4.15 Check for stresses at construction stage (1,2) in interior I-girder:

| Properties | Values (Mpa) | | | | | |
|----------------------|--------------|------|------|------|------|------|
| | 0 | 2.7 | 5.4 | 8.1 | 10.8 | 13.5 |
| Section from end (m) | 0 | 2.7 | 5.4 | 8.1 | 10.8 | 13.5 |
| σ _{top} | 4.53 | 7.95 | 7.21 | 7.06 | 7.95 | 8.43 |
| σ _{bottom} | 6.75 | 11.2 | 12.9 | 13.8 | 13.1 | 12.7 |

Table 4.16 Check for stresses at construction stage (2,2) in interior I-girder:

| Properties | Values (Mpa) | | | | | |
|----------------------|--------------|------|------|------|------|------|
| | 0 | 2.7 | 5.4 | 8.1 | 10.8 | 13.5 |
| Section from end (m) | 0 | 2.7 | 5.4 | 8.1 | 10.8 | 13.5 |
| σ _{top} | 4.57 | 8.06 | 7.43 | 7.40 | 8.32 | 8.81 |
| σ _{bottom} | 6.55 | 10.4 | 11.6 | 12.3 | 11.4 | 10.9 |

Table 4.17 Check for stresses at construction stage (2,3) in interior I-girder:

| Properties | Values (Mpa) | | | | | |
|----------------------|--------------|------|------|------|------|------|
| | 0 | 2.7 | 5.4 | 8.1 | 10.8 | 13.5 |
| Section from end (m) | 0 | 2.7 | 5.4 | 8.1 | 10.8 | 13.5 |
| σ _{top} | 3.41 | 5.74 | 5.52 | 5.68 | 6.29 | 6.61 |
| σ _{bottom} | 6.25 | 9.14 | 9.73 | 9.77 | 9.00 | 8.62 |

Table 4.18 Check for stresses at construction stage (3,1) in interior I-girder:

Table 4.19 Check for stresses at service stage (SLS) in interior I girder:

| Properties | Values (Mpa) | | | | | |
|----------------------|--------------|------|------|------|------|------|
| | 0 | 2.7 | 5.4 | 8.1 | 10.8 | 13.5 |
| Section from end (m) | 0 | 2.7 | 5.4 | 8.1 | 10.8 | 13.5 |
| σ _{top} | 3.38 | 5.74 | 5.52 | 5.68 | 6.29 | 6.61 |
| σ _{bottom} | 6.25 | 6.82 | 6.19 | 5.13 | 4.23 | 3.53 |

As all stress values in all construction stages are within permissible limit i.e. 16 Mpa and 12.8 Mpa compressive stresses in transfer stage and working stage respectively. 0 Mpa tensile stresses in all construction stages or there is no tensile stress at all in any stage.

Table 4.20 Check for deflection at various stages in interior I girder:

| Stages | Deflection (mm) | | | | | |
|----------------------|-----------------|------|-------|-------|-------|-------|
| | 0L | 0.1L | 0.2L | 0.3L | 0.4L | 0.5L |
| Section from end (m) | 0 | 2.7 | 5.4 | 8.1 | 10.8 | 13.5 |
| Stage (1,1) | 0 | 4.96 | 9.37 | 12.38 | 13.76 | 13.76 |
| Stage (1,2) | 0 | 2.71 | 5.18 | 6.64 | 7.09 | 7.09 |
| Stage (2,2) | 0 | 5.28 | 9.79 | 12.56 | 13.62 | 13.62 |
| Stage (2,3) | 0 | 6.10 | 11.22 | 14.38 | 15.61 | 15.60 |
| Stage (3,2) | 0 | 9.64 | 17.31 | 21.99 | 23.86 | 23.86 |

The above all deflection values are within limits 34mm i.e. (span/800) so, it is safe in deflection criteria.

5. Conclusion:

An attempt has been made in the present study to understand the current design practice of PSC I-type Girder Superstructure bridge using MIDAS civil software in which construction stage wise analysis are carried out as per construction sequences of the bridge. The following observations and conclusions are made from this project work.

Alternative 4 numbers of longitudinal girders of 1.4m depth with 3 nos. of prestressing cable 19K15 used in simply supported structure.

- it is found that compressive stress value is 3.24 Mpa in exterior girder and no tensile stress at any stages. maximum deflection is 20mm.
- it is found that compressive stress value is 3.53 Mpa in interior girder and no tensile stress at any stages. maximum deflection is 24mm.

References:

- [1] Abhyankar, V.G. (2011). "Bridge Erection Techniques and their Influence on Permanent Designs", *National Workshop on "Innovation in Bridge Engineering"*, at COEP, Pune.
- [2] Abhyankar, V.G. (2011). "Nad-Al-Sheba Race Course development Project: Construction of Three Bridges." *ISSE Journal*, Vol.13-2.
- [3] Ahsan, R., Rana, S., and Ghani, S.N. (2012). "Cost Optimum Design of Posttensioned I-Girder Bridge using Global Optimization Algorithm", *Journal of Structural Engineering*, ASCE, 138(2).
- [4] Hodson, D.J., Barr, P.J., and Halling, M.W. (2012). "Live-Load Analysis of Posttensioned Box-Girder Bridges", *Journal of Bridge Engineering*, ASCE, 17(4).
- [5] IRC:6-(2014). *Standard specifications and code of practice for Road Bridges, Section: II Loads and Stresses*, The Indian Roads Congress, New Delhi, India.
- [6] IRC:18-(2000). *Design criteria for Prestressed Concrete Road Bridges (Post-tensioned Concrete) (Third Revision)*, The Indian Roads Congress, New Delhi, India.
- [7] IRC:112-(2011). *Standard specifications and code of practice for Road Bridges, Section: II, Loads and Stresses*, The Indian Roads Congress, New Delhi, India.
- [8] IS 1343:1980. *Prestressed concrete code of practice (second revision)*, Indian Standard, New Delhi, India.
- [9] Krishna Raju, N. (1995). "Prestressed Concrete", Tata McGraw-Hill Publishing Company Limited, New Delhi.
- [10] Laskar, A., Howser, R., Mo, Y.L., and Hsu, T.T.C. (2010). "Modeling of Prestressed Concrete Bridge Girders", *Journal of Earth and Space*, ASCE.
- [11] Oh, B.H., and Yang, I.H. (2001). "Realistic Long-Term Prediction of Prestress Forces in PSC Box Girder Bridges", *Journal of Structural Engineering*, ASCE, 127(9).